

The Crystal Structure of Dicalcium Phosphate, CaHPO_4

BY G. MACLENNAN AND C. A. BEEVERS

Chemistry Department, University of Edinburgh, Scotland

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Anhydrous dicalcium phosphate has been found to be triclinic with space group $P\bar{1}$, the cell dimensions being

$$a = 6.90 \pm 0.01, \quad b = 6.65 \pm 0.01, \quad c = 7.00 \pm 0.01 \text{ \AA};$$

$$\alpha = 96^\circ 21', \quad \beta = 103^\circ 54', \quad \gamma = 88^\circ 44'.$$

The atomic coordinates have been found by analysis of the three-dimensional Patterson function, and the structure has been refined to a residual error factor $R = 0.20$. The structure contains independent PO_4 groups, one kind of calcium atom having a coordination of seven and the other of eight oxygens. Visual estimates of intensities were employed and the errors in these are considered to be too large to enable the positions of the hydrogen atoms to be found.

Introduction

The crystal structure of anhydrous dicalcium phosphate, CaHPO_4 , (calcium hydrogen phosphate, or monetite) was investigated as part of a programme of research into phosphate structures of interest both in fertilizer manufacture and in the complex subject of phosphate fixation in the soil. A description of the structure of dicalcium phosphate dihydrate, $\text{CaHPO}_4 \cdot 2\text{H}_2\text{O}$, has already been given (Beever & Raistrick, 1954). The work is being undertaken in collaboration with the Research Department of Scottish Agricultural Industries Ltd.

The substance CaHPO_4 is of particular interest as it is the form present in several mixed fertilizers, especially those in whose manufacture nitric acid and/or free ammonia are used. It is hoped that the work, of which this structure determination is a part, will help to make more intelligible the changes which occur during manufacture and in the soil, and especially to clarify the nature of the solids deposited from solution with Ca/P ratios in the range between 1.0 (dicalcium phosphate) and 1.66 (hydroxyapatite).

Experimental

According to Groth (1908) anhydrous dicalcium phosphate is triclinic pinacoidal. Exceptionally pure prismatic crystals of maximum size 0.5 mm. were kindly made available by the Research Department of the Tennessee Valley Authority. Oscillation and Weissenberg photographs about the principal axes were obtained, using $\text{Cu } K\alpha$ radiation and a 5 cm.-radius normal-beam Weissenberg camera. The unit-cell dimensions were obtained from high-order $0kl$, $h0l$ and $hk0$ reflexions. The results were

$$a = 6.90 \pm 0.01, \quad b = 6.65 \pm 0.01, \quad c = 7.00 \pm 0.01 \text{ \AA};$$

$$\alpha = 96^\circ 21', \quad \beta = 103^\circ 54', \quad \gamma = 88^\circ 44'.$$

These agree with the values previously obtained by Lehr, Smith & Brown (1952).

The cell contains four molecules of CaHPO_4 , giving a calculated specific gravity of 2.92, compared with observed values of 2.93 (de Schulten) and 2.89 (Bassett). The space-group is $P\bar{1}$, and we have confirmed the presence of the morphological centre of symmetry by the statistical test of Howells, Phillips & Rogers (1950).

The reflexion intensities were estimated by visual comparison, using multiple exposures, and were corrected for Lorentz and polarization factors. The small irregular crystals precluded any correction for the rather high absorption. An attempt was made to place the intensities for the three two-dimensional zones on an absolute scale by Wilson's method, but this proved unsatisfactory, probably because of the absorption effect. The latter also prevented any measurement of the temperature factor. The general intensities were therefore left on a relative scale.

Structure determination

In the space group $P\bar{1}$ the general positions are two-fold, and, since there are two CaHPO_4 molecules in the unique volume of the cell, all the atoms can be in general positions. Since there are only four unique heavy atoms, giving rise to sixteen interatomic vectors, Patterson methods seemed promising. The three Patterson projections down the principal axes were computed, but the occurrence of many almost coincident vectors made their interpretation impossible.

A three-dimensional Patterson function over the unique half of the cell was therefore calculated, using an electrical analogue computer of the Hägg-Laurent type, built by Dr F. Stern. Intervals of 30ths of the cell edges were used, and the resulting function was drawn out in 16 sections parallel to the b - c plane. A list was drawn up of the principal vectors, and a

Table 1. Values of F_o and F_c for the $(hk0)$, $(h0l)$, $(0kl)$ and $(hk3)$ planes of Ca_2HPO_4

hkl	F_o	F_c	hkl	F_o	F_c	hkl	F_o	F_c	hkl	F_o	F_c	hkl	F_o	F_c	hkl	F_o	F_c	hkl	F_o	F_c	hkl	F_o	F_c									
010	0	$\bar{1}$	$\bar{2}\bar{3}$	0	1	500	29	$\bar{3}\bar{0}$	810	14	20	207	4	8	$4\bar{0}\bar{6}$	19	$\bar{1}\bar{5}$	$7\bar{0}\bar{7}$	28	$\bar{1}\bar{7}$	$0\bar{6}\bar{2}$	38	38	055	34	$\bar{4}\bar{3}$	213	64	65	$\bar{3}\bar{3}\bar{3}$	13	$\bar{7}$
020	32	25	$\bar{4}\bar{4}$	39	41	510	21	$\bar{2}\bar{0}$	820	3	7	208	0	1	$4\bar{0}\bar{7}$	16	15	801	28	$\bar{1}\bar{3}$	$0\bar{7}\bar{2}$	10	$\bar{1}\bar{2}$	065	20	17	313	0	1	$\bar{4}\bar{3}\bar{3}$	0	7
030	51	$\bar{5}\bar{1}$	$\bar{2}\bar{5}$	27	$\bar{2}\bar{0}$	520	37	$\bar{3}\bar{8}$	830	10	15	201	54	$\bar{6}\bar{4}$	408	5	2	801	20	17	082	7	$\bar{4}$	015	11	6	413	42	$\bar{3}\bar{6}$	533	0	0
040	33	$\bar{3}\bar{1}$	$\bar{2}\bar{6}$	35	32	530	12	$\bar{6}$	810	12	$\bar{1}\bar{2}$	202	78	77	501	36	$\bar{3}\bar{3}$	802	23	28	013	0	0	025	19	$\bar{1}\bar{6}$	513	0	$\bar{5}$	$\bar{6}\bar{3}\bar{3}$	28	$\bar{4}$
050	23	14	$\bar{2}\bar{7}$	12	$\bar{8}$	540	8	$\bar{9}$	820	16	$\bar{1}\bar{8}$	203	0	2	502	35	30	803	33	$\bar{3}\bar{7}$	023	30	$\bar{1}\bar{1}$	035	0	$\bar{6}$	613	32	27	733	0	8
060	10	7	$\bar{2}\bar{8}$	15	12	550	28	27	830	7	$\bar{3}$	204	38	$\bar{3}\bar{7}$	503	7	6	804	16	$\bar{1}\bar{9}$	033	44	$\bar{3}\bar{7}$	045	6	6	713	20	18	143	24	$\bar{1}\bar{8}$
070	6	$\bar{6}$	300	24	18	560	27	29	001	21	$\bar{2}\bar{0}$	205	0	$\bar{1}$	504	20	$\bar{2}\bar{0}$	805	30	31	043	67	$\bar{3}\bar{7}$	055	21	20	113	24	$\bar{1}\bar{1}$	143	6	8
080	16	$\bar{2}\bar{4}$	310	47	$\bar{4}\bar{4}$	510	0	3	002	62	$\bar{8}\bar{9}$	206	8	9	505	0	$\bar{6}$	011	10	10	053	33	29	065	21	$\bar{1}\bar{6}$	213	27	$\bar{3}\bar{5}$	243	35	$\bar{1}\bar{9}$
100	0	2	320	21	$\bar{2}\bar{3}$	520	8	$\bar{9}$	003	53	63	207	0	$\bar{3}$	501	0	7	021	14	$\bar{1}\bar{4}$	063	5	$\bar{3}$	075	23	$\bar{2}\bar{1}$	313	29	18	343	0	3
110	0	3	330	16	14	530	6	8	004	20	20	208	0	3	502	18	$\bar{2}\bar{2}$	031	15	8	073	29	34	016	46	52	413	21	20	443	0	$\bar{4}$
120	64	83	340	12	12	540	25	$\bar{2}\bar{7}$	005	9	$\bar{1}\bar{0}$	301	46	47	503	40	30	041	40	32	013	40	$\bar{4}\bar{1}$	026	0	2	513	0	5	343	6	7
130	42	$\bar{4}\bar{0}$	350	25	$\bar{1}\bar{5}$	550	0	$\bar{9}$	006	0	$\bar{1}$	302	0	$\bar{4}$	504	0	5	051	24	$\bar{1}\bar{5}$	023	23	$\bar{1}\bar{4}$	036	0	2	613	0	$\bar{6}$	643	30	$\bar{2}\bar{7}$
140	5	0	360	30	$\bar{2}\bar{7}$	560	24	20	007	0	7	303	28	$\bar{2}\bar{2}$	505	42	$\bar{3}\bar{9}$	061	39	46	033	50	$\bar{4}\bar{7}$	046	0	$\bar{9}$	713	0	0	743	0	3
150	5	3	370	19	$\bar{1}\bar{1}$	600	30	34	008	0	$\bar{2}$	304	11	9	506	17	14	071	16	$\bar{1}\bar{7}$	043	16	22	056	22	24	813	0	$\bar{1}$	153	29	$\bar{1}\bar{9}$
160	23	18	310	28	$\bar{2}\bar{9}$	610	0	7	101	19	$\bar{1}\bar{9}$	305	38	36	507	18	12	081	9	$\bar{1}\bar{2}$	053	18	12	016	24	23	123	69	69	153	53	50
170	29	20	320	88	93	620	0	$\bar{5}$	102	49	$\bar{4}\bar{5}$	306	0	$\bar{6}$	508	14	$\bar{1}\bar{0}$	011	15	16	063	62	61	026	38	$\bar{3}\bar{9}$	223	23	20	253	44	$\bar{4}\bar{3}$
180	19	19	330	0	$\bar{4}$	630	18	$\bar{1}\bar{3}$	103	18	24	307	28	$\bar{3}\bar{8}$	601	55	53	021	19	20	073	0	0	036	37	$\bar{3}\bar{7}$	323	74	$\bar{6}\bar{6}$	353	37	$\bar{2}\bar{1}$
110	0	$\bar{6}$	340	47	54	640	32	$\bar{3}\bar{6}$	104	21	25	301	22	22	602	14	$\bar{1}\bar{6}$	031	50	60	083	12	14	046	0	$\bar{8}$	423	0	4	453	0	6
120	69	$\bar{9}\bar{3}$	350	11	$\bar{1}\bar{0}$	650	11	11	105	20	$\bar{1}\bar{3}$	302	17	18	603	19	$\bar{1}\bar{7}$	041	39	$\bar{4}\bar{5}$	014	34	$\bar{3}\bar{8}$	056	27	$\bar{2}\bar{7}$	523	20	14	553	0	$\bar{8}$
130	24	23	360	5	$\bar{5}$	660	12	$\bar{1}\bar{3}$	106	5	$\bar{5}$	303	0	$\bar{3}$	604	16	11	051	8	$\bar{7}$	024	8	$\bar{1}\bar{1}$	066	24	22	623	10	$\bar{1}\bar{6}$	653	0	3
140	7	$\bar{6}$	370	0	$\bar{1}$	610	0	0	107	4	5	304	42	39	601	53	$\bar{7}\bar{0}$	061	60	$\bar{6}\bar{0}$	034	0	$\bar{2}$	017	31	$\bar{3}\bar{3}$	123	70	$\bar{8}\bar{1}$	163	35	25
150	25	15	400	5	4	620	8	$\bar{8}$	108	0	$\bar{3}$	305	12	15	602	9	6	071	6	8	044	0	5	027	14	$\bar{1}\bar{2}$	223	36	42	263	0	0
160	6	2	410	17	$\bar{1}\bar{6}$	630	23	$\bar{2}\bar{8}$	101	9	$\bar{5}$	306	40	$\bar{3}\bar{8}$	603	61	75	081	0	2	054	0	$\bar{6}$	037	0	5	323	0	$\bar{2}$	363	37	$\bar{3}\bar{5}$
170	29	$\bar{2}\bar{0}$	420	20	22	640	18	18	102	31	25	307	4	$\bar{1}\bar{5}$	604	19	$\bar{1}\bar{8}$	012	26	25	064	9	$\bar{7}$	047	15	$\bar{1}\bar{3}$	423	0	$\bar{1}\bar{2}$	463	24	$\bar{2}\bar{7}$
180	16	$\bar{1}\bar{7}$	430	19	22	650	0	0	103	48	$\bar{4}\bar{7}$	308	23	22	605	17	$\bar{1}\bar{3}$	022	39	$\bar{3}\bar{2}$	074	16	$\bar{1}\bar{0}$	017	17	$\bar{1}\bar{7}$	523	51	64	173	10	$\bar{2}\bar{6}$
200	78	$\bar{8}\bar{8}$	440	23	22	660	56	59	104	40	$\bar{2}\bar{5}$	401	55	$\bar{3}\bar{5}$	606	19	22	032	29	19	014	20	$\bar{1}\bar{6}$	027	25	26	623	0	$\bar{3}$	273	34	$\bar{1}\bar{3}$
210	13	8	450	8	11	700	10	19	105	14	13	402	10	4	607	0	$\bar{8}$	042	17	15	024	60	66	037	0	$\bar{8}$	723	34	$\bar{4}\bar{3}$			
220	16	$\bar{1}\bar{7}$	460	7	13	710	18	27	106	9	12	403	34	32	701	4	7	052	21	$\bar{1}\bar{5}$	034	37	36	047	22	$\bar{1}\bar{6}$	823	0	10			
230	6	4	470	22	$\bar{1}\bar{5}$	720	30	39	107	0	0	404	18	11	702	28	$\bar{2}\bar{2}$	062	0	7	044	34	$\bar{2}\bar{5}$	057	8	$\bar{1}\bar{3}$	133	42	$\bar{4}\bar{3}$			
240	0	$\bar{8}$	410	19	$\bar{1}\bar{9}$	730	9	$\bar{1}\bar{0}$	108	0	5	405	16	$\bar{1}\bar{1}$	703	0	4	072	15	13	054	22	20	018	10	$\bar{1}\bar{4}$	233	38	42			
250	41	$\bar{3}\bar{1}$	420	0	6	740	0	$\bar{3}$	201	62	72	406	0	$\bar{2}$	701	9	$\bar{1}\bar{4}$	082	18	27	064	34	$\bar{3}\bar{9}$	028	8	10	333	30	40			
260	35	$\bar{3}\bar{5}$	430	11	11	710	0	1	202	6	$\bar{4}$	401	55	59	702	0	$\bar{9}$	012	9	8	074	25	25	018	30	$\bar{3}\bar{0}$	433	20	17			
270	10	11	440	28	$\bar{2}\bar{9}$	720	18	$\bar{2}\bar{5}$	203	58	$\bar{6}\bar{1}$	402	55	$\bar{4}\bar{3}$	703	8	$\bar{1}\bar{2}$	022	47	$\bar{6}\bar{1}$	015	50	47	028	5	8	533	15	$\bar{1}\bar{2}$			
280	19	20	450	0	$\bar{2}$	730	5	$\bar{1}\bar{0}$	204	0	9	403	39	$\bar{3}\bar{8}$	704	4	8	032	6	$\bar{6}$	025	26	27	038	0	10	633	0	$\bar{8}$			
210	21	21	460	47	$\bar{4}\bar{8}$	740	16	15	205	18	13	404	44	44	705	20	21	042	12	17	035	0	1	048	30	26	133	35	35			
220	25	19	470	15	14	800	33	$\bar{4}\bar{2}$	206	0	$\bar{6}$	405	17	$\bar{2}\bar{0}$	706	0	$\bar{2}$	052	0	1	045	33	40	113	7	6	233	27	18			

preliminary attempt was made to recover the fundamental set of heavy atoms from them by trial and error. This failed, as in many previous instances, and the vector-convergence method of Beever & Robertson (1950) was adopted. This involved using three or more heavy atoms to search for the relative positions of the remainder in the cell, and then noting the centre of symmetry, and hence the absolute positions by inspection. Heavy atoms were assumed to lie at the Patterson origin and at two other outstandingly high peaks, and the Patterson function was superposed over the entire cell with these positions in turn as origin. The coincidence of vectors at once revealed the other five heavy atoms and the centre of symmetry, showing that the original two vectors had been correctly chosen. Moreover, by observing the peak heights carefully, Ca and P atoms were unambiguously separated.

It yet remained to discover the sixteen O atoms. The number of recorded coincidences of medium height corresponding to possible oxygen positions was confusingly large, and a further superposition with a fourth heavy atom failed to simplify the choice. The fact that the P-O distance is approximately 1.6 Å was therefore used. Spheres of this radius were constructed round the four P atoms, and all coincident vectors within about 0.2 Å of the spheres were noted. Pairs of these which were related by the previously-found centre of symmetry were then picked out. Nine pairs were in fact found, of which one corresponded to an atom in a sterically impossible position near the centre, and the remaining eight gave convincing PO_4 tetrahedra with no gross packing difficulties. All the vectors between the heavy atoms and the oxygens chosen were then calculated and compared with the

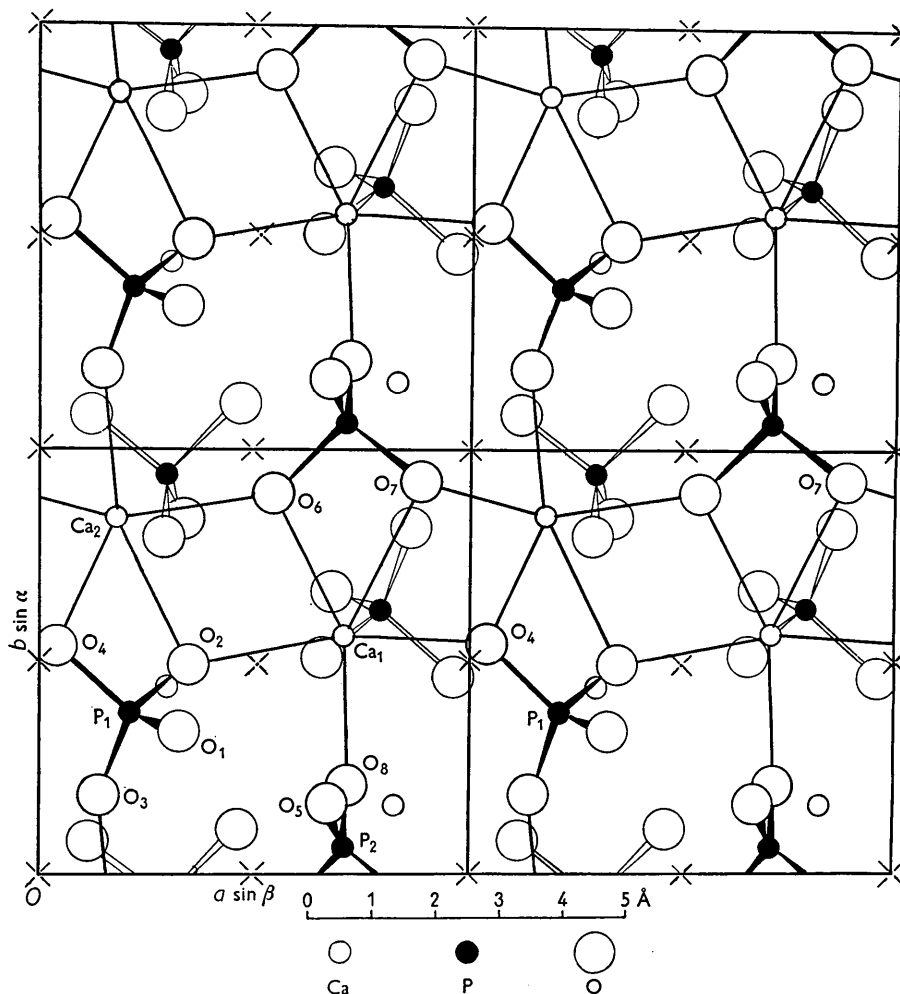


Fig. 1. Four unit cells of CaHPO_4 , projected down the c axis.

original Patterson function to ensure not only that all the vectors were present, but that no significant peaks on the map remained unaccounted for. This was confirmed, and small alterations were then applied to the atomic positions to obtain the best possible overall fit.

Refinement

The atomic positions obtained were used to calculate structure factors for the $(0kl)$ zone. This gave encouraging agreement, the factor $R = \sum ||F_o| - |F_c|| \div \sum |F_o|$ being 0.40. A Fourier projection, using the 77 F_o terms which could be signed, showed satisfactory details and only small shifts. When these were applied R fell to 0.35. Further refinement was carried out by the use of $(F_o - F_c)$ syntheses, F_o being first scaled to fit F_c over five ranges of $\sin \theta$, since the Wilson scaling curve was not felt to be reliable. Four stages of refinement reduced R to 0.203. It was then decided to refine the x parameters using the $(hk0)$ zone. Structure factors calculated using the x parameters from the Patterson superposition and the already refined y parameters

gave $R = 0.51$. Five stages of refinement exactly as for the previous zone reduced this to $R = 0.196$. Finally the $(h0l)$ zone was refined and the structure factors calculated for the three zones with the mean parameters from the three refinements. The residuals were then:

$$R(hk0) = 0.193, R(h0l) = 0.216, R(0kl) = 0.193; \\ \text{average } R = 0.201.$$

These figures include reflexions of observed zero intensity, and no corrections have been applied for extinction nor for a temperature factor. As a final check of the validity of the structure, structure factors for the $(hk3)$ planes were calculated. Satisfactory agreement was obtained with $R = 0.285$. Observed and calculated F values for the planes $(hk0)$, $(h0l)$, $(0kl)$ and $(hk3)$ are given in Table 1.

Fourier projections computed for the final structure showed the oxygen atoms badly distorted by the diffraction rings round the heavy atoms. This is to be expected when the Fourier series for atoms with no heat motion is abruptly terminated, and the effect

could be reduced by the introduction of a suitable temperature factor.

The final atomic parameters, in 360ths of the cell edges, are:

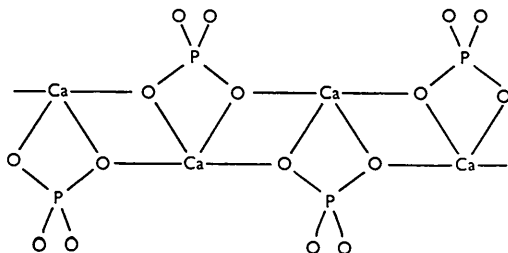
	<i>x</i>	<i>y</i>	<i>z</i>
Ca ₁	106	157	98
Ca ₂	63	302	240
P ₁	74	135	259
P ₂	107	339	75
O ₁	114	120	336
O ₂	123	177	222
O ₃	48	66	213
O ₄	15	192	270
O ₅	120	300	6
O ₆	165	39	108
O ₇	39	27	57
O ₈	105	285	126

The accuracy of the determination was estimated using the equations given by Cruickshank (1949). The standard deviation in electron density, $\sigma(\rho)$, is $1.1 \text{ e.}\text{\AA}^{-2}$ on the $(0kl)$ projection. The standard deviation in atomic coordinates in the *c* direction, $\sigma(z)$, is 0.006 \AA for Ca, 0.011 \AA for P and 0.039 \AA for O. Hence the standard deviations in bond lengths are:

Ca-O = 0.039 \AA ,
 P-O = 0.040 \AA ,
 O-O = 0.055 \AA ,
 O-O = 0.078 \AA (if related by a centre of symmetry).

Description of the structure

The structure of Ca_2HPO_4 consists of discrete PO_4^{3-} tetrahedra and Ca^{2+} ions, the latter coordinated by a shell of oxygen atoms. Fig. 1 shows a projection of the structure down the *c* axis, four unit cells being shown. In the *a* direction Ca₁ is bonded to O₂ and O₄ attached to P₁, while Ca₂ is bonded to O₆ and O₇, attached to P₂. In the *b* direction Ca₁ is bonded to O₆ and O₇, and Ca₂ to O₂ and O₄, so that a double chain of Ca-PO₄-Ca extends along the *a* axis, thus:



Bonds from Ca₁ to O₆ and Ca₂ to O₃ link these chains transversely in the *b* direction, forming a distorted sheet of atoms roughly in the (001) plane. The centre of symmetry produces a similar sheet below the first in the *c* direction, further bonds from Ca₁ to O₁' and O₂', and from Ca₂ to O₃', O₅' and O₈' linking the sheets. Ca₁ thus has seven and Ca₂ eight nearest oxygen neighbours in its coordination shell. This variation in the calcium coordination is not unexpected. The

highly electropositive nature of the metallic ion results in an unusually great ionic character in its coordination, so that no definite allocation of shared electrons from the oxygens is possible. Ca-O coordinations of all values from 6 to 9 have been reported (see Wells, 1945) and different values in the same structure have been noted where the symmetry permits (Smith, 1953).

The bond lengths and angles obtained are given in Table 2.

The average P-O bond length is 1.54 \AA , the average Ca-O bond length is 2.46 \AA , and the average distance O-O within the PO₄ group is 2.51 \AA .

The two hydrogen atoms probably lie between oxygens of neighbouring PO₄ groups. It is not feasible to identify their positions by a reduction in the O-O distance between non-bonded atoms, since in this case, with a standard deviation of 0.055 \AA in the bond length, only differences in O-O bonds greater than 0.18 \AA are significant. This uncertainty, caused primarily by the swamping effect of the heavy atoms, is sufficient

Table 2. Bond lengths and angles

P ₁ -O ₁ = 1.53 \AA	Ca ₁ -O ₁ ' = 2.44 \AA	Ca ₂ -O ₂ = 2.58 \AA
P ₁ -O ₂ = 1.58	Ca ₁ -O ₂ = 2.34	Ca ₂ -O ₃ = 2.40
P ₁ -O ₃ = 1.49	Ca ₁ -O ₂ ' = 2.48	Ca ₂ -O ₃ ' = 2.43
P ₁ -O ₄ = 1.56	Ca ₁ -O ₄ = 2.29	Ca ₂ -O ₄ = 2.44
P ₂ -O ₅ = 1.52	Ca ₁ -O ₆ = 2.44	Ca ₂ -O ₅ = 2.44
P ₂ -O ₆ = 1.56	Ca ₁ -O ₇ = 2.69	Ca ₂ -O ₆ = 2.51
P ₂ -O ₇ = 1.55	Ca ₁ -O ₈ = 2.37	Ca ₂ -O ₇ = 2.58
P ₂ -O ₈ = 1.54		Ca ₂ -O ₈ ' = 2.51

O ₁ -P ₁ -O ₂ = 116.5°	O ₅ -P ₂ -O ₆ = 111.0°
O ₁ -P ₁ -O ₃ = 113.5	O ₅ -P ₂ -O ₇ = 109.0
O ₁ -P ₁ -O ₄ = 105.5	O ₅ -P ₂ -O ₈ = 107.0
O ₂ -P ₁ -O ₃ = 108.5	O ₆ -P ₂ -O ₇ = 100.0
O ₂ -P ₁ -O ₄ = 103.5	O ₆ -P ₂ -O ₈ = 108.5
O ₂ -P ₁ -O ₄ ' = 116.0	O ₇ -P ₂ -O ₈ = 112.0

to obscure any evidence of hydrogen bonding. In fact, the shortest measured O-O contact is 2.48 \AA between O₇ and its symmetry-related atom, where the standard deviation is higher [$\sigma(d_{12}) = 2\sigma(x_1)$] and where a hydrogen bond is not possible by space-group considerations. The next shortest contacts observed are

$$\text{O}_1-\text{O}_5 = 2.60, \text{O}_6-\text{O}_8' = 2.62, \text{O}_4-\text{O}_7 = 2.71 \text{ \AA}.$$

The structure of Ca_2HPO_4 is thus a three-dimensional network of PO_4^{3-} tetrahedra with Ca^{2+} ions in the interstices, holding the anions together by highly ionic bonds with the oxygens. There seems to be no close resemblance to the structures of chemically related compounds, though CaSO_4 , which is orthorhombic, has very similar cell dimensions (Dickson & Binks, 1926). In particular, the structure of apatite (Beever & MacIntyre, 1946) is quite different, so that profound alterations in the crystal lattice must be necessary as the Ca/P ratio is reduced from 1.66, and a continuous series of solid solutions between hydroxyapatite and anhydrous dicalcium phosphate seems unlikely.

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The Crystal Structure of Hydroxylamine

BY EDWARD A. MEYERS AND WILLIAM N. LIPSCOMB

School of Chemistry, University of Minnesota, Minneapolis 14, Minnesota, U.S.A.

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Four molecules of hydroxylamine are in an orthorhombic unit cell of symmetry $P2_12_12_1$ and dimensions $a = 7.29$, $b = 4.39$, $c = 4.88$ Å. The coordinates $x_O = 0.060$, $y_O = -0.062$, $z_O = -0.023$, $x_N = 0.121$, $y_N = 0.244$ and $z_N = 0.063$ lead to the N-O bond distance of $1.47_6 \pm 0.03$ Å, and to the closest intermolecular contacts of $N \cdots O = 2.74$, 3.07 , 3.11 and 3.18 Å. Hydrogen bonds are presumed to lie in the 2.74 and 3.07 Å contacts, thus leaving the third hydrogen atom of the molecule uninvolved, and indicating a *trans* configuration for the molecule. No residual entropy is indicated, and no transition occurs when the solid is cooled to -185° C.

Introduction

Two spectroscopic investigations of hydroxylamine, one of the solid and gas by Giguère & Liu (1952), and one of the solid at low temperature by Nightingale & Wagner (1954), have recently been made. These studies differ somewhat in the observations, and the assignments of the bands are different. In particular, Nightingale & Wagner assigned the broad, intense band at 2867 cm.^{-1} to a strong hydrogen bond.

In the hope that we could provide some information relating to these spectroscopic studies, and in the expectation that the structure might be closely related to those shown by hydrazine (Collin & Lipscomb, 1950, 1951), hydrogen peroxide (Abrahams, Collin & Lipscomb, 1951), methanol (Tauer & Lipscomb, 1952), and methylamine (Atoji & Lipscomb, 1953), we have carried out a study of the crystal structure as described below. Low-temperature techniques were employed partly because of the low melting point of 33° C., but chiefly because of the tendency towards rapid decomposition near room temperature.

Experimental

Hydroxylamine, prepared by the method of Hurd (1939), was transferred to a vacuum line and was

partially further purified by pumping out volatile impurities for periods up to 30 min. The usual techniques of sublimation into capillaries produced impure samples, so that a modified technique was used. A section of glass tubing between the sample and vacuum pumps was drawn down to capillary diameter. With the pumps maintained in operation, a short length of this constricted region was cooled to near liquid-nitrogen temperature, allowed to warm for a short time, cooled again, with the low-temperature stream of nitrogen, and then sealed on both sides of the small slug of solid hydroxylamine. Thus prepared, the samples were stored in dry ice.

X-ray diffraction data were collected on the precession camera from a single crystal, grown with the use of a warm air stream, and maintained at -60° C. during photography. Mo $K\alpha$ radiation was used, and precession angles of 21° for the $\{h0l\}$ zone and 30° for the $\{hko\}$, $\{0kl\}$, $\{hkh\}$ and $\{2h,k,h\}$ zones were employed. No X-ray diffraction evidence of a phase transition was observable at temperatures down to -185° C.

Intensities were estimated visually with the use of a standard scale of timed exposures of a reflection from a crystal of NaCl of comparable size. The usual Lorentz and polarization corrections (Waser, 1951)